

On the asymmetry of velocity oscillation amplitude in bipolar active regions

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ABSTRACT

The velocity field in the lower solar atmosphere undergoes strong interactions with magnetic fields. Many authors have pointed out that power is reduced by a factor between two and three within magnetic regions, depending on frequency, depth, the radius and the magnetic strength of the flux tube. Many mechanisms have been proposed to explain the observations. In this work, SDO dopplergrams and magnetograms of 12 bipolar active regions (β ARs) at a 45 second cadence, are used to investigate the relation between velocity fluctuations and magnetic fields. We show that there is an asymmetry within β ARs, with the velocity oscillation amplitude being more suppressed in the leading polarities compared to the trailing polarities. Also, the strongest magnetic fields do not completely suppress the five-minute oscillation amplitude, neither in the spot innermost umbrae.

Key words. Sun:activity, Sun: oscillations

1. Introduction

The study of the interaction between waves and magnetic fields plays an important role in the investigation of the mechanisms responsible for the solar corona heating.

It is well established that the amplitude of solar five-minute oscillations in the photosphere is reduced by a factor of two to three within ARs (Leighton et al. 1962; Woods & Cram 1981; Lites et al. 1982; Abdelatif et al. 1986; Braun et al. 1987; Tarbell et al. 1988; Braun et al. 1988; Title et al. 1992; Hindman & Brown 1998). The reduction is observed to depend on frequency, depth, and on the physical parameters that describe the flux tubes, i.e. their radius and magnetic strength (Brown et al. 1992; Hindman & Brown 1998; Gordovskyy & Jain 2008). This behavior has been also found in small magnetic field concentrations (Roberts & Webb 1978; Spruit 1981; Bogdan et al. 1996; Cally & Bogdan 1997; Hindman & Jain 2008; Jain et al. 2009; Hindman & Jain 2012; Pradeep Chitta et al. 2012).

It is also known that at higher frequencies, above the acoustic cutoff frequency in the low photosphere, the velocity oscillations amplitude is enhanced at the edges of ARs (Braun et al. 1992; Brown et al. 1992; Toner & Labonte 1993). Also, an enhancement of power in the three-minute band has recently been observed in the inner umbra of a pore (Stangalini et al. 2012).

Several mechanisms have been proposed to explain the observations (Hindman et al. 1997):

1) The intrinsic power inhibition due to local convection suppression. By using numerical simulations Parchevsky & Kosovichev (2007) found that the reduction of wave excitation in a sunspot, can account up to 50% of the power deficit.

2) Partial p-mode absorption (Braun et al. 1987; Bogdan et al. 1993; Cally 1995; Cally & Andries 2010). Spruit & Bogdan (1992) showed that the wave absorption by sunspots can be

interpreted in terms of p-modes mode conversion between the oscillations and MHD waves. Both models (Cally & Bogdan 1993) and simulations (Cameron et al. 2008) have shown that mode conversion is able to remove a significant amount of energy from the incident helioseismic wave, with an efficiency that depends on the angle of the magnetic field from the vertical, with a maximum at about 30° (Cally et al. 2003; Crouch & Cally 2003).

3) Opacity effects. Within a magnetic region, the line-of-sight optical depth experiences a depression (Wilson depression). Due to increasing density, the amplitude of the velocity fluctuations decrease with depth.

4) Alteration of the p-mode eigenfunctions at the hands of the magnetic field (Jain et al. 1996; Hindman et al. 1997).

We note that the majority of the studies on the interaction between solar oscillations and magnetic field have focused on the use of models and simulations.

Because of the dependence of the velocity amplitude on magnetic strength, the most noticeable effects are observed within ARs, where the strongest magnetic fields are found. Among them, bipolar active regions (hereafter β ARs) are particularly interesting, showing asymmetries in their morphology and physical properties, as several works have already pointed out (see, e.g., Bray & Loughhead 1979; Balthasar & Woehl 1980; Ternullo et al. 1981; Zwaan 1985; van Driel-Gesztelyi & Petrovay 1990; Petrovay et al. 1990; Fan et al. 1993). Moreno-Insertis et al. (1994) conclude that morphological asymmetries are due to the different inclination with which the polarities of β ARs emerge.

Using simulations, Fan et al. (1993) have studied area asymmetries, and predict that the leading polarity must have a strength about twice larger than the trailing polarity, at the same depth. This result, which is a consequence of the Coriolis force action on the magnetic structure, is able to account for the trailing spot fragmentation, its lower flux magnitude and shorter lifetime.

MDI observations of 138 bipolar magnetic regions have recently

quantitatively shown that the areas of leading polarities are typically smaller than those of trailing polarities (Yamamoto 2012). This area asymmetry could be produced by the Coriolis force during a flux tube's rising motion in the solar convection zone.

In this work we investigated the velocity oscillation amplitude reduction by the magnetic field within β ARs. We analyzed 12 β ARs from SDO-HMI data, both in the Northern (N) and Southern (S) hemispheres, and we found that the leading polarity systematically has a greater reduction in amplitude than the trailing. In addition, we studied the amplitude reduction as a function of the field inclination for AR11166.

2. SDO-HMI data

Our data set consists of 12 SDO-HMI magnetograms and dopplergrams pairs with 1 arcsec spatial resolution (Scherrer et al. 2012; Schou et al. 2012). These were acquired with a 45 second cadence, which set the Nyquist frequency. Each β AR data set is 3 hours long, which set the lower cut-off at $\sim 10^{-4} s^{-1}$. Observation times cover the interval from 2011 March 8 to 2012 January 3 (see Table 1).

We selected 8 isolated bipolar regions in the N hemisphere, and 4 in the S hemisphere. In order to limit the effects due to the inclination with respect to the line-of-sight, we selected β ARs as close as possible to the disk center. The rectangular area enclosing the β ARs was selected such that it included all the magnetic features with strength above 500 G, with the minimum and maximum allowed dimensions of the enclosing rectangle being 500 and 700 arcseconds, respectively. Figure 1 shows the mean magnetograms of two selected β ARs: AR 11166 in the N hemisphere, AR 11316 in the S hemisphere. In both panels the leading polarity is on the right and it is negative for the Northern β ARs, positive for the Southern β ARs. Table 1 shows the list of β ARs analyzed in this work.

3. Method and analysis

The selected regions around each β AR were co-registered using a FFT technique ensuring sub-pixel accuracy. Inspection of the co-registered data shows that the strong magnetic structures remain in the same position during the entire duration of the acquisition. The amplitude of velocity oscillations was estimated pixel-by-pixel through their integrated spectrum. Specifically, we selected a spectral window $\Delta\nu$ centered at 3 mHz (five-minute band), having a width of 1 mHz, and then we integrated the FFT amplitude spectrum A_ν in that frequency range

$$A_{xy} = \int_{\Delta\nu} A_\nu d\nu$$

We then divided the data into bins of magnetic field, each 25 G wide, and averaged the amplitude of velocity oscillations in each bin, thus obtaining $A_B = \langle A_{xy} \rangle_B$. We consider only pixels with $|\mathbf{B}| > 25$ G. Since all the amplitude distributions within the respective magnetic bin have a Gaussian-like shape (see inset in Figure 2b), we use σ/\sqrt{n} as error on A_B , where σ is the standard deviation and n are the counts in each bin.

4. Results and Discussion

4.1. Oscillation amplitude VS magnetic field strength

In Figure 2 we show the integrated amplitude A_{xy} scatter plot (black dots), and A_B for each magnetic bin (red line), for the

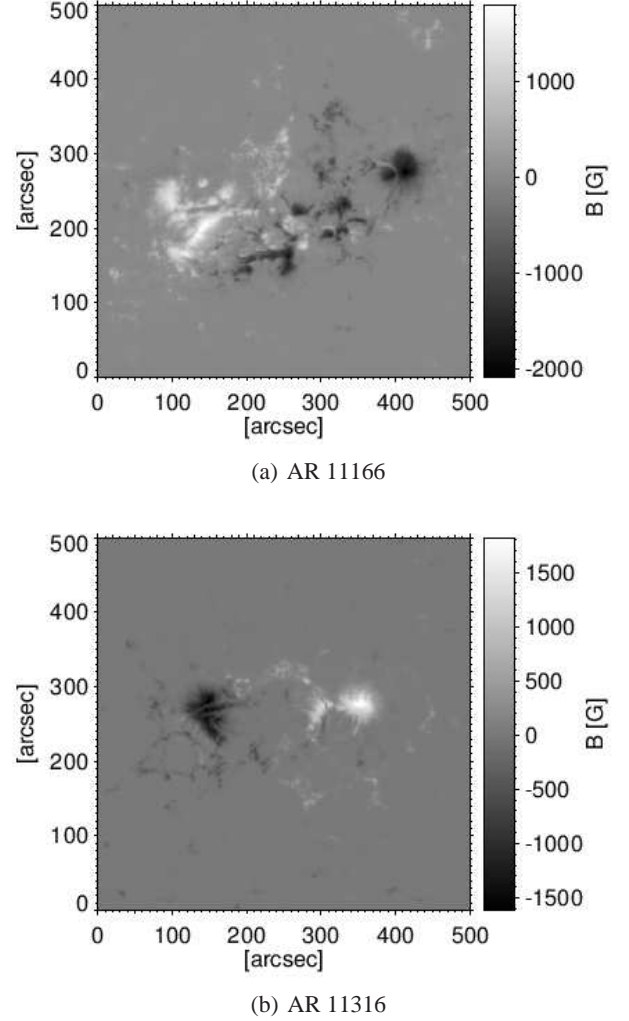


Fig. 1. SDO-HMI mean magnetograms of (a) AR 11166 (b) AR 11316. See Table 1 for more details.

β ARs shown in Figure 1. Hereafter, we refer to the A_B plot as the amplitude profile. The amplitude shows a decreasing trend up to a plateau, that is almost always reached in the range 0.5-1 kG (as in the case of Figure 2b). This feature suggests that the amplitude is independent of the magnetic field strength above a threshold value, which is different for each β AR and each polarity in the same β AR.

For every polarity present in the 12 β ARs analyzed, we computed the oscillation amplitude reduction as the ratio $d = A_{1000}/A_{25}$, where A_{1000} and A_{25} are, respectively, the mean oscillation velocity around $B = 1000$ G, and that around $B = 25$ G, the minimum observable strength. Averaging the d values over all the β ARs, we obtained $\bar{d} = 0.54 \pm 0.06$, which agrees with the oscillation amplitude reductions in magnetic environments quoted in the literature (e.g. Woods & Cram 1981; Lites et al. 1982; Braun et al. 1987; Tarbell et al. 1988).

The plateau in the amplitude profiles for high B values, is intriguing. By visual inspection, we verified that it takes place almost exclusively in the β AR spot umbrae, as can be expected given the high magnetic field values. We can exclude an instrumental effect, since the magnetic strength threshold changes with each β AR and even with the polarity in the same β AR, and we are well above the 20 m/s error on the velocity

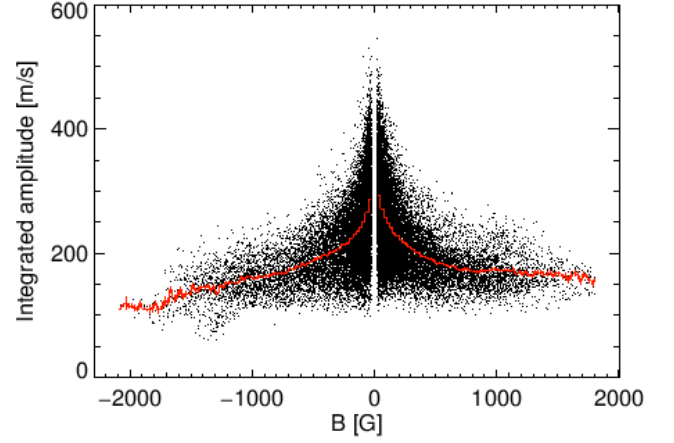
Table 1. Details of SDO-HMI data used. The fourth column shows the leading to trailing polarity area ratio.

β AR number	Observation Date	Location	S_l/S_t
AR11166	2011.03.08	N11 W01 T11:00-14:00	0.88
AR11283	2011.09.05	N13 W01 T17:00-20:00	0.86
AR11302	2011.09.28	N13 W06 T17:30-20:30	0.96
AR11319	2011.10.15	N09 E02 T07:00-10:00	0.95
AR11316	2011.10.15	S12 E01 T07:00-10:00	0.90
AR11330	2011.10.27	N09 E04 T18:30-21:30	0.83
AR11338	2011.11.06	S14 W00 T20:00-23:00	0.92
AR11341	2011.11.11	N08 W00 T07:00-10:00	1.05
AR11362	2011.12.03	N08 W06 T20:00-23:00	1.10
AR11367	2011.12.07	S18 W05 T20:00-23:00	0.90
AR11375	2011.12.13	N08 W03 T19:00-22:00	0.82
AR11389	2012.01.03	S22 W05 T16:00-19:00	0.97

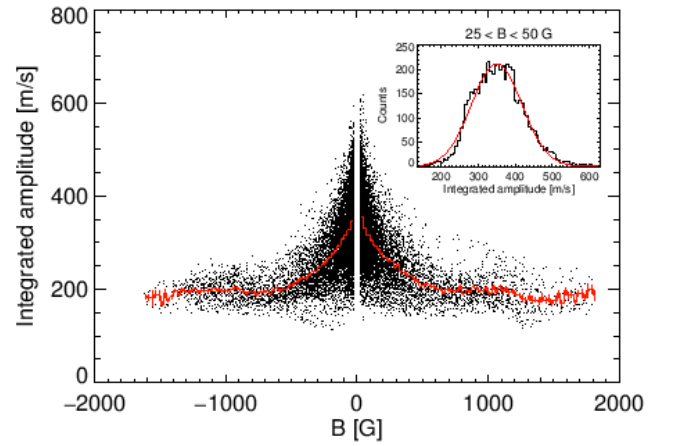
measurements due to the HMI filter transmission profiles (Fleck et al. 2011). It seems that the oscillation amplitudes are not completely suppressed even in the strongest magnetic fields, and are not dependent on the magnetic field strength anymore. Conversely to the simulations of Cattaneo et al. (2003), it may indicate a saturation effect of the kinetic energy in the strong field regime, and shed new light onto the mechanisms that co-operate in the reduction of acoustic power in the lower atmosphere.

4.2. The leading-trailing asymmetry

To investigate the relations between local oscillation amplitude and magnetic field strength, we compute the midpoints of the amplitude profiles. Specifically, we draw horizontal lines at constant A_B values, proceeding down in steps of 10 m/s. We compute the abscissa of each midpoint on the segment that intersects the amplitude profiles. If these profiles were symmetric, the midpoints should be on the $B = 0$ vertical line. In order to compare the amplitude profiles from different β ARs, we normalize them to their average value A_B in the $B = \pm 25$ G bins. We remind that, for solar cycle 24, the leading polarities are negative in the N hemisphere and positive in the S hemisphere. Figure 3a shows the midpoint lines for all the 12 β ARs considered in this study. Northern and Southern β AR families appear well defined and separated. Moreover, as can be seen in Figure 3, the amount of asymmetry, defined as the distance of each midpoint from the vertical line through $B = 0$, increases for stronger fields. In the N hemisphere (in blue) it extends up to $|B| \approx 230$ G, while in S hemisphere (in red) it is less apparent, and only reaches $|B| \approx 130$ G. The amplitude profiles of Northern β ARs are biased toward positive polarities, i.e. the trailing, while the Southern β ARs are biased toward negative polarities, i.e. the trailing again.



(a) AR 11166



(b) AR 11316

Fig. 2. In panel a) the integrated velocity oscillation amplitude for AR11166 is shown; the same for AR1136 in panel b). The red overplots correspond to the average in each magnetic field bin. In the inset of panel b) amplitude distribution in the $25 < B < 50$ G bin (black line) and gaussian fit (red line) are shown.

To visualize differently the asymmetry, we can fix a value $|B|$ for the magnetic strength, and compute the amplitude difference, i.e. the difference between the respective averaged amplitudes for both polarities in each β AR, namely $A_{|B|} - A_{-|B|}$. In Figure 3b we show these differences versus the absolute value of magnetic strength for all β ARs of Table 1. This plot confirms that the asymmetry is lower where the field is weaker. At 25 G the difference is about 10 m/s and typical values for velocity amplitudes up to 600 m/s; at 1000 G the difference rises to over 50 m/s, while the amplitudes are ~ 200 m/s. Both in N and S hemispheres the oscillation amplitude in the trailing polarity is higher than that in the leading polarity. This fact implies that $A_{|B|} > A_{-|B|}$ in the N hemisphere and viceversa in the S hemisphere, and that the amplitude reduction is less efficient in the trailing polarity.

Such an asymmetry suggests that the amount of oscillation reduction within magnetic environments is not a function of the local magnetic field strength only. If this were the case, we would observe the same oscillation amplitudes for B and $-B$ magnetic fields. This would imply both the plots of Figure 3 to

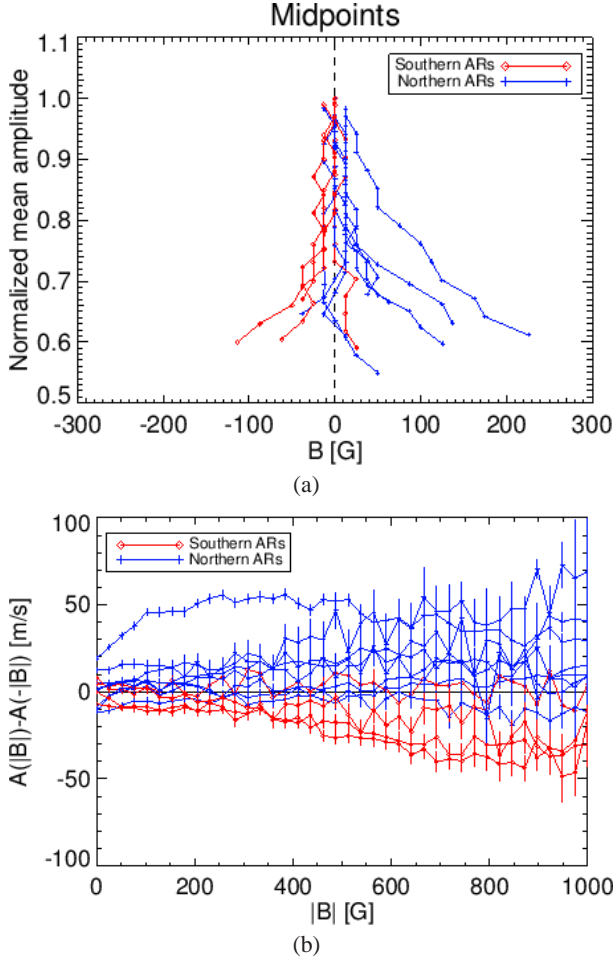


Fig. 3. a) Midpoints for normalized velocity oscillations amplitude. b) Difference between oscillation amplitude for both polarities against the magnetic strength. Bars represent errors. Red line with diamonds, refers to Southern β ARs, blue line with plus signs to Northern β ARs.

lie on the line through 0 G (a) and 0 m/s (b), respectively.

The simulations of Fan et al. (1993) about area asymmetries of β ARs, predicted a pronounced difference in the field strength between the leading and the trailing polarities, and ensuing differences in their fragmentation and lifetimes. This suggests that the asymmetry we found could derive from non-local properties, i.e. on the whole magnetic environment topology and even its surroundings.

We therefore computed the area asymmetry in our magnetograms following Yamamoto (2012), with a threshold $B > 500$ G. The results are reported in the fourth column of Table 1. We found that, on average, the area of the leading polarity is $\sim 90\%$ of the trailing polarity area, regardless the hemisphere which the β AR belongs to. This quantifies how much a trailing polarity is spread with respect to its leading polarity. We can speculate that a relation may exist between the area and the oscillation suppression, due to a different interaction of acoustic waves with sparser or denser active region polarities.

4.3. Oscillation amplitude VS magnetic field inclination

The case of AR11166

To support the findings reported in sec. 4.2, we studied the dependence of the oscillation amplitude on the magnetic field inclination angle θ in an β AR. For this purpose, we considered the AR11166 (Figure 1a) as a case study. We used the LOS inclination maps provided by the VFISV (Very Fast Inversion of the Stokes Vector, Borrero et al. 2011) inversion of HMI vector magnetic field data.

In Figure 4 we show the magnetic field inclination map of

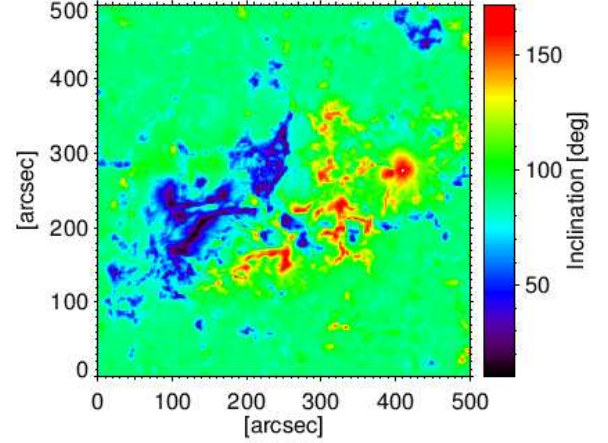


Fig. 4. Inclination map of AR 11166. The leading polarity (negative) ranges from 90° to 180° , and the trailing polarity (positive) from 0° to 90° .

AR11166. The inclinations retrieved by the VFISV span the range $10^\circ < \theta < 172^\circ$. Following the most used sign convention, the leading polarity (negative) ranges from 90° to 180° , and the trailing polarity (positive) from 0° to 90° . As expected, the innermost umbrae are mostly line of sight, as the β ARs were selected as close as possible to the disk center.

VFISV also provides the error σ_θ associated to the inclination, for each pixel (Borrero et al. 2011; Press et al. 1986). To avoid polarity flips due to the inversion error, we discarded all those pixels where $\theta \pm 3\sigma_\theta$ causes the field to flip its inclination from positive to negative (or vice-versa). We stress that VFISV is a Milne-Eddington code, therefore blind to any B and v line of sight gradients, which produce asymmetries in the Stokes profiles. This happens most often in regions filled by weak fields (Viticchié et al. 2011; Viticchié & Sánchez Almeida 2011). Moreover, the inversion of low signal to noise Stokes profiles is usually problematic (see Landi Degl’Innocenti 1992; Borrero et al. 2011, for more details). For noisy Stokes profiles, and therefore low B values, VFISV (and any inversion code) tends to be biased toward $\sim 90^\circ$ inclinations (Borrero & Kobel 2011). For these reasons and to be consistent with the threshold used in 3, we rejected the pixels with $B < 25$ G and $75^\circ < \theta < 105^\circ$. After this selection, about 17% of the initial pixels were selected for the analysis.

We plotted A_{xy} and its average in each θ bin $A_\theta = \langle A_{xy} \rangle_\theta$ against the magnetic field inclination θ (shown in Figure 5). For ease of comparison, in the upper panel of Figure 6 we show again A_θ versus θ in the range $[10^\circ, 75^\circ]$. Both A_θ smoothly decrease from ~ 250 m/s to ~ 140 m/s, from almost horizontal to almost vertical fields, respectively, but the oscillation amplitude reduction is more effective for the leading polarity (red curve)

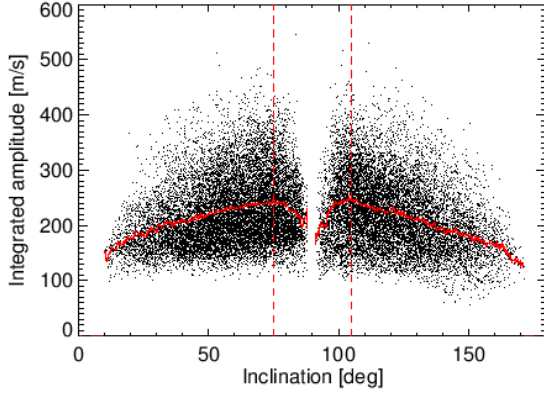


Fig. 5. Integrated velocity oscillation amplitude within AR11166 as a function of the magnetic field inclination θ . The thick red line corresponds to the average amplitude $A_\theta = \langle A_{xy} \rangle_\theta$ in each θ bin ($\Delta\theta = 1^\circ$). The vertical dashed lines mark the threshold $\theta < 75^\circ$ OR $\theta > 105^\circ$.

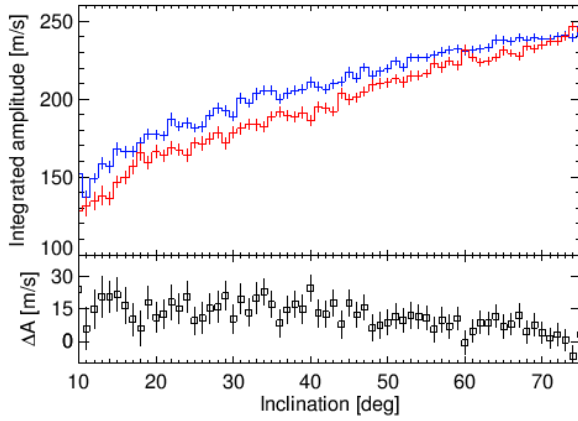


Fig. 6. Upper panel: A_θ^T and A_θ^L versus θ in the range $[10^\circ, 75^\circ]$. The blue line represents the average amplitude of the positive (trailing) polarity: A_θ^T . The red line represents the average amplitude of the negative (leading) polarity after a remapping operation: $\theta \rightarrow 180^\circ - \theta$: A_θ^L . Lower panel: ΔA versus θ (see the text). Vertical bars represent the error, which were computed for each A_θ with the same method described in section 3, and then summed up.

than for the trailing polarity (blue curve).

In the lower panel of Figure 6 we plot the oscillation amplitude asymmetry $\Delta A = A_\theta^T - A_\theta^L$ VS θ . ΔA is constant (≈ 15 m/s) within the errors up to $\theta \approx 45^\circ$, then ΔA drops to very few m/s. The inclination analysis shows that a ≈ 15 m/s asymmetry exists between the polarities of AR11166. In particular, the velocity oscillation amplitude is enhanced in the trailing polarity with respect to the leading.

There is no evident relation between the asymmetry ΔA and the inclination θ . For any $\theta \lesssim 45^\circ$ the oscillation amplitude asymmetry is positive and around 15 m/s. We interpret the drop at $\approx 45^\circ$ as the combined effect of the VFISV preference to associate weak fields with larger inclinations (Borrero & Kobel 2011), and of the amplitude difference to be small for weak fields (see Figure 3b). Also, an incorrectly retrieved weak B may result due to unresolved mag-

netic structuring in the pixel (e.g. Sánchez Almeida 1998; Socas-Navarro & Sánchez Almeida 2003; Viticchié et al. 2011), and we recall that a VFISV hypothesis is that the magnetic field is constant within the pixel.

Schunker & Cally (2006) and Stangalini et al. (2011) have demonstrated that, due to mode conversion, there exists a preferred angle at which the power is significantly larger. In our case, we indeed focus on the amplitude asymmetry between the two polarities, instead of considering the proper amplitude dependence that may be affected by biases due to the magnetic field strength.

5. Conclusions

In this work we focused on the velocity oscillation amplitude reduction in β ARs, reaching the following conclusions.

The oscillation amplitude reduction found in magnetic environments of β ARs is 0.54 ± 0.06 , which agrees with the values quoted in the literature (e.g. Woods & Cram 1981; Lites et al. 1982; Braun et al. 1987; Tarbell et al. 1988).

The five-minute amplitudes are not completely suppressed in the strongest magnetic fields of the spot innermost umbra. It would be very important to understand why a plateau appears in the oscillation amplitude profiles for strong fields.

There exists a leading-trailing polarity asymmetry in β ARs. The asymmetry suggests that the reduction in oscillation amplitude does not depend on the field strength only, but may depend also on non-local conditions, such as the area on which the field spreads, for instance.

The trailing polarity systematically shows a higher oscillation amplitude than the leading polarity, regardless the hemisphere which the β AR belongs to.

The plot of the velocity oscillation amplitude as a function of the magnetic field inclination confirms such an asymmetry in β ARs. Apparently, the asymmetry does not evidently depend on the inclination.

We took advantage from HMI full-disk data at a 45 s time cadence, and at 1 arcsec spatial resolution. The analysis of these data revealed a possible saturation of the oscillation amplitude reduction for strong B , and an asymmetry in such a reduction for leading-trailing polarities. These results have to be accounted for in modeling the power reduction in magnetic environments, the emergence and the evolution of β ARs.

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